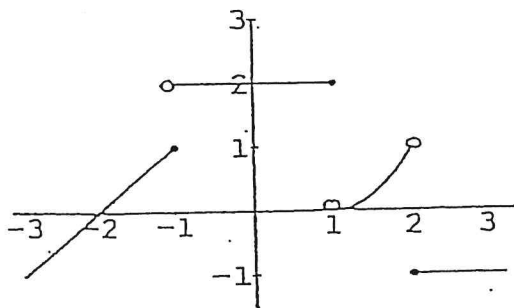


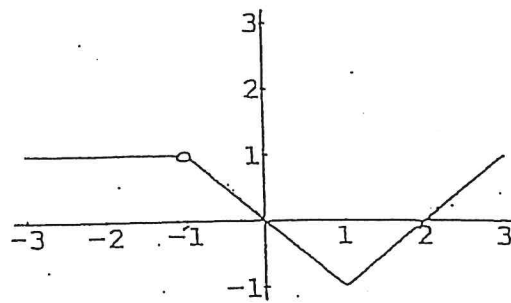
CALCULUS
WORKSHEET ON LIMITS

from Calculus Problems for a New Century

1. The graphs of the functions f and g are given below.



graph of f



graph of g

Determine whether the following limits exist. If they do, then find the limit.

a. $\lim_{x \rightarrow -1} f(x)$

b. $\lim_{x \rightarrow 1} f(x)$

c. $\lim_{x \rightarrow -1} g(x)$

d. $\lim_{x \rightarrow 1} g(x)$

e. $\lim_{x \rightarrow -1} [f(x) + g(x)]$

f. $\lim_{x \rightarrow 0} [2f(x) + 3g(x)]$

g. $\lim_{x \rightarrow -1} [f(x)g(x)]$

h. $\lim_{x \rightarrow 2} [f(x)g(x)]$

i. $\lim_{x \rightarrow 0} \frac{f(x)}{g(x)}$

j. $\lim_{x \rightarrow 0} \frac{g(x)}{f(x)}$

k. $\lim_{x \rightarrow -2} g(f(x))$

l. $\lim_{x \rightarrow -1} f(g(x))$

2. The graphs of functions f and g are those given in Problem 1 above. Determine whether the following limits exist and find the limit when it exists.

a. $\lim_{x \rightarrow -1^-} f(x)$

b. $\lim_{x \rightarrow -1^+} f(x)$

c. $\lim_{x \rightarrow -1^-} g(x)$

d. $\lim_{x \rightarrow -1^+} g(x)$

e. $\lim_{x \rightarrow 0^-} f(x + 2)$

f. $\lim_{x \rightarrow -1^-} f(x^2)$