

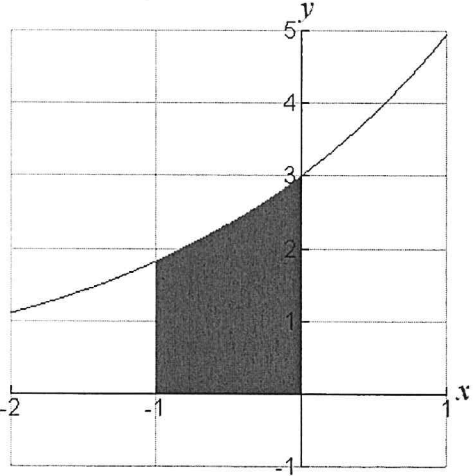
1. The functions $f(x) = 2 - x^2$ and $g(x) = -x$ are given.

<p>a. Find the area of the region bounded by the graphs of $f(x)$ and $g(x)$.</p> $\int_{-1}^2 [(2 - x^2) - (-x)] dx =$ $\int_{-1}^2 (2 - x^2 + x) dx =$ $2x - \frac{x^3}{3} + \frac{x^2}{2} \Big _{-1}^2 = \frac{9}{2}$	<p>+2: integrand</p> <p>+1: limits & answer</p>
<p>b. Find the area of the region bounded by the graph of $f(x)$ and the x-axis.</p> $\int_{-\sqrt{2}}^{\sqrt{2}} (2 - x^2) dx = 2x - \frac{x^3}{3} \Big _{-\sqrt{2}}^{\sqrt{2}}$ $= 4\sqrt{2} - \frac{4\sqrt{2}}{3}$	<p>+2: integral</p> <p>+1: answer</p>
<p>c. Find the area of the region bounded by the graph of $g(x)$, the x-axis and the line $x = 2$.</p> $\int_0^2 [0 - (-x)] dx = 2$	<p>+2 integral</p> <p>+1: answer</p>

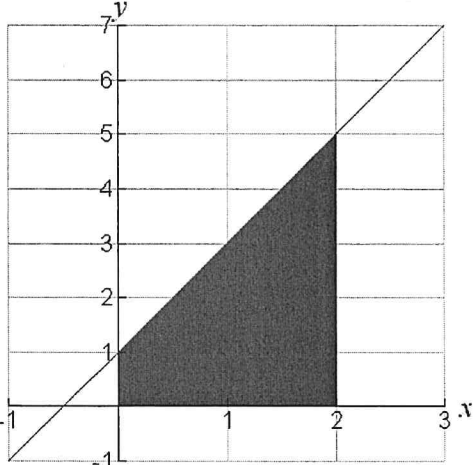
2. The functions $f(x) = x^2 - 2$ and $g(x) = x$ are given.

<p>a. Find the area of the region(s) bounded by the graphs of $f(x)$, the y-axis and the x-axis.</p> <p>The area of the first region is given by</p> $\int_0^{\sqrt{2}} [0 - (x^2 - 2)] dx = \int_0^{\sqrt{2}} (-x^2 + 2) dx$ $= -\frac{x^3}{3} + 2x \Big _0^{\sqrt{2}}$ $= \frac{4\sqrt{2}}{3}$ <p>The second region, which is to the left of the y axis, has the same area. So the total area is $\frac{8\sqrt{2}}{3}$.</p>	<p>+2: integral</p> <p>+1: answer</p>
<p>b. Find the area of the region bounded by the graphs of $f(x)$ and $g(x)$.</p> $\int_{-1}^2 [x - (x^2 - 2)] dx =$ $\frac{x^2}{2} - \frac{x^3}{3} + 2x \Big _{-1}^2 = \frac{9}{2}$	<p>+2: integral</p> <p>+1: answer</p>
<p>c. Find the area of the region bounded by the graph of $g(x)$ and the x-axis between the lines $x = -2$ and $x = 1$.</p> $\int_{-2}^0 (0 - x) dx + \int_0^1 x dx = \frac{5}{2}$	<p>+2: integral</p> <p>+1: answer</p>

3. $F(y) = \int_{-1}^y 3e^{x/2} dx$

<p>a. Find the accumulation function F.</p> $\int_{-1}^y 3e^{x/2} dx = 6e^{x/2} \Big _{-1}^y$ $= 6e^{y/2} - 6e^{-1/2}$	<p>+2: antiderivative</p> <p>+1: answer</p>
<p>b. Evaluate $F(-1)$, $F(0)$, and $F(4)$.</p> $F(-1) = 0$ $F(0) = 6 - 6e^{-1/2}$ $F(4) = 6e^2 - 6e^{-1/2}$	<p>+1 for 0</p> <p>+1 for $6 - 6e^{-1/2}$</p> <p>+1 for $6e^2 - 6e^{-1/2}$</p>
<p>c. Graphically show the area given by the value $F(0)$.</p> 	<p>+2: graph of $3e^{x/2}$</p> <p>+1: shaded area</p>

4. $F(x) = \int_0^x (2t+1)dt$

<p>a. Find the accumulation function F.</p> $\int_0^x (2t+1)dt =$ $t^2 + t \Big _0^x = x^2 + x$	<p>+2: antiderivative</p> <p>+1: answer</p>
<p>b. Evaluate $F(0)$, $F(2)$, and $F(6)$.</p> $F(0) = 0$ $F(2) = 6$ $F(6) = 42$	<p>+1: 0</p> <p>+1: 6</p> <p>+1: 42</p>
<p>c. Graphically illustrate the area given by the value $F(2)$.</p> 	<p>+2: graph of $y = 2t + 1$</p> <p>+1: shaded area</p>

5. Consider the region bounded by the graphs of $f(x) = \sqrt{x}$, $y = 0$, and $x = 2$.

<p>a. Find the volume of the solid formed by rotating the region about the x-axis.</p> $\pi \int_0^2 (\sqrt{x})^2 dx =$ $\pi \frac{x^2}{2} \Big _0^2 = 2\pi \approx 6.283$	<p>+2: integral</p> <p>+1: limits, constant, answer</p>
<p>b. Find the volume of the solid formed by rotating the region about the y-axis.</p> $\pi \int_0^{\sqrt{2}} (4 - y^4) dy =$ $\pi \left(4y - \frac{y^5}{5} \right) \Big _0^{\sqrt{2}} = \frac{16\sqrt{2}}{5} \pi \approx 14.217$	<p>+2: integral</p> <p>+1: limits, constant, answer</p>
<p>c. Find the volume of the solid formed by rotating the region about the line $y = -2$.</p> $\pi \int_0^2 \left[(\sqrt{x} + 2)^2 - 4 \right] dx =$ $\pi \int_0^2 (x + 4\sqrt{x} + 4 - 4) dx =$ $\pi \left(\frac{x^2}{2} + \frac{8}{3} x^{3/2} \right) \Big _0^2 =$ $\left(2 + \frac{16}{3} \sqrt{2} \right) \pi \approx 29.979$	<p>+2: integral</p> <p>+1: limits, constant, answer</p>

6. Consider the region bounded by $y = x^3$, $y = 8$, and $x = 0$.

<p>a. Find the volume of the solid formed by rotating the region about the y-axis</p> $\pi \int_0^8 (\sqrt[3]{y})^2 dy =$ $\pi \left(\frac{3}{5} y^{5/3} \right) \Big _0^8 = \frac{96}{5} \pi \approx 60.319$	<p>+2: integrand +1: limits, constant, answer</p>
<p>b. Find the volume of the solid formed by rotating the region about the x-axis.</p> $\pi \int_0^2 (8^2 - (x^3)^2) dx =$ $\pi \int_0^2 (64 - x^6) dx =$ $\pi \left[64x - \frac{x^7}{7} \right] \Big _0^2 = \frac{768}{7} \pi \approx 344.678$	<p>+2: integrand +1: limits, constant, answer</p>
<p>c. Find the volume of the solid formed by rotating the region about the line $x = 2$.</p> $\pi \int_0^8 (2^2 - (2 - \sqrt[3]{y})^2) dy =$ $\pi \int_0^8 (4y^{1/3} - y^{2/3}) dy =$ $\pi \left[3y^{4/3} - \frac{3}{5} y^{5/3} \right] \Big _0^8 =$ $\pi \left[3(16) - \frac{3}{5}(32) \right] = \frac{144}{5} \pi \approx 90.478$	<p>+2: integrand +1: limits, constant, answer</p>