

p. 146 Find $\frac{dy}{dx}$ by implicit differentiation.

$$(2) \quad x^2 - y^2 = 25$$

$$2x - 2y \frac{dy}{dx} = 0$$

$$2x = 2y \frac{dy}{dx}$$

$$\frac{2x}{2y} = \frac{dy}{dx}$$

$$\frac{x}{y} = \frac{dy}{dx}$$

$$(6) \quad x^2y + y^2x = -2$$

$$2x \cdot y + x^2 \frac{dy}{dx} + 2y \frac{dy}{dx} \cdot x + y^2 = 0$$

$$x^2 \frac{dy}{dx} + 2xy \frac{dy}{dx} = -y^2 - 2xy$$

$$\frac{dy}{dx} (x^2 + 2xy) = -y^2 - 2xy$$

$$\frac{dy}{dx} = \frac{-y^2 - 2xy}{x^2 + 2xy}$$

$$(14) \quad \cot y = x - y$$

$$-\frac{dy}{dx} \csc^2 y = 1 - \frac{dy}{dx}$$

$$\frac{dy}{dx} - \frac{dy}{dx} \csc^2 y = 1$$

$$\frac{dy}{dx} (1 - \csc^2 y) = 1$$

$$\frac{dy}{dx} = \frac{1}{-\cot^2 y} = -\tan^2 y$$

$$(10) \quad 4(\cos x \sin y) = 1$$

$$-4 \sin x \sin y + \frac{dy}{dx} \cos y \cdot 4(\cos x) = 0$$

$$\frac{dy}{dx} \cdot 4(\cos x \cos y) = 4 \sin x \sin y$$

$$\frac{dy}{dx} = \frac{4 \sin x \sin y}{4 \cos x \cos y}$$

$$\frac{dy}{dx} = \tan x \tan y$$

$$(30) \quad (4-x)y^2 = x^3 \text{ at } (2, 2)$$

$$4y^2 - xy^2 = x^3$$

$$8y \frac{dy}{dx} - [y^2 + x \cdot 2y \frac{dy}{dx}] = 3x^2$$

$$16 \frac{dy}{dx} - [4 + 8 \frac{dy}{dx}] = 3 \cdot 4$$

$$\frac{8dy}{dx} = 16$$

$$\frac{dy}{dx} = 2$$

$$(28) \quad x(\cos y) = 1$$

at $(2, \pi/3)$

$$\cos y + x(-\sin y) \frac{dy}{dx} = 0$$

$$\cos \pi/3 = 2 \sin \pi/3 \cdot \frac{dy}{dx}$$

$$1/2 = 2 \cdot \sqrt{3}/2 \cdot \frac{dy}{dx}$$

$$\frac{1}{2\sqrt{3}} = \frac{dy}{dx}$$

(42) a) $\frac{x^2}{6} - \frac{y^2}{8} = 1$ at $(3, -2)$

$$\frac{2x}{6} - \frac{2y}{8} \frac{dy}{dx} = 0$$

$$\frac{x}{3} - \frac{y}{4} \cdot \frac{dy}{dx} = 0$$

$$\frac{3}{3} = \frac{-2}{4} \frac{dy}{dx}$$

$$1 = -\frac{1}{2} \frac{dy}{dx}$$

$$-2 = \frac{dy}{dx}$$

Tangent Line

$$y + 2 = -2(x - 3)$$

$$y + 2 = -2x + 6$$

$$y = -2x + 4$$

Normal Line:

$$y + 2 = \frac{1}{2}(x - 3)$$

(34) $(x+2)^2 + (y-3)^2 = 37$ at $(4, 4)$

$$2(x+2) + 2(y-3) \frac{dy}{dx} = 0$$

$$2(6) + 2(1) \frac{dy}{dx} = 0$$

$$2 \frac{dy}{dx} = -12$$

$$\frac{dy}{dx} = -6$$

$$y - 4 = -6(x - 4)$$

$$y - 4 = -6x + 24$$

$$y = -6x + 28$$